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VISUALIZATION OF ACOUSTIC WAVES PROPAGATING WITHIN A SINGLE ANISOTROPIC CRYSTALLINE PLATE

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Abstract: We present a hybrid acoustic imaging system to directly visualize acoustic waves propagating within a single anisotropic crystalline plate. A high frequency acoustic point focus lens was used to form a small point source within the plate. A laser interferometric system was used to visualize the acoustic wave propagation. Distinct amplitude patterns at each focal plane were experimentally visualized. The patterns are also theoretically calculated with an Angular Spectrum of Plane Waves method.

Key words: Laser Based Ultrasonics, Acoustic Lens, Angular Spectrum, Anisotropy

Introduction

The mechanical scanning acoustic reflection microscope (hereinafter called simply "SAM") operating with frequencies substantially ranging from 0.1 to 2.0GHz has proven to be a useful apparatus for characterizing of anisotropic materials on the scale of individual grains [1-3]. Note that the SAM is basically designed to visualize the surface and/or the subsurface of microstructure features

of the material, but not directly the acoustic waves propagating within the material. However, observing a wave front traveling within the material would be significant for understanding physical phenomena, such as scattering from microstructure features [4-7]. In addition, visualization of the acoustic wave front can help in measurement of elastic properties and improve quality evaluation of an acoustic lens.

In this article, we present a hybrid imaging system comprising laser based acoustic microscopy and scanning acoustic microscopy for directly visualizing wave front amplitudes of acoustic bulk and surface waves emanating from a focused source outside and inside a material sheet. A high frequency (~200 MHz) acoustic lens tightly focused compression waves onto the back surface of a thin silicon plate, crystalline plane (100) oriented with its normal to the plate surface, via a coupling medium (*i.e.*, distilled water). A laser beam focused onto the front surface of the specimen via an optical objective lens included in the laser interferometric system detected the amplitudes of the bulk and surface acoustic waves at the front surface of the plate. Distinct symmetric amplitude patterns that altered in predictable ways, as the acoustic focal point moved toward the front surface of the plate, were observed. Predictions of the acoustic wave fields generated by the acoustic lens within the plate are being investigated with an Angular Spectrum of Plane Waves method for an anisotropic crystalline solid [8-10].

Theoretical Approach

We adopt "Angular-Spectrum of Plane Waves" approach [10] to predict the acoustic wave amplitude at the surface of the silicon plate taking into account all the modes excited through. If the wave amplitude or stress distribution is known on any plane, then the corresponding wave amplitude or stress can be calculated on any other parallel plane through a summation of plane waves propagating form one plane to the other. Each plane wave component must be a solution to the appropriate wave equation for the medium through which it travels. Since the angular frequency and the parameters of the acoustic lens are known, the acoustic field focused on the back surface plane can be calculated. The summation must occur over all in-plane components of wave-number and include propagating as well as non-propagating wave-vectors. The main complication to this approach is that the Christoffel equation must be solved for the z-component of the wave-vector that satisfies for the frequency used and all the in-plane wave-vector components. In this way, the acoustic displacement amplitude on any plane in the water and inside or at the

surface of the silicon plate can be calculated with reflectance and transmission functions.

Experiment

Figure 1 illustrates a schematic diagram of the experimental measurement. The optoacoustic system comprises a computer for controlling all operations and data acquisition, a laser interferometric system based on the photorefractive effect, a detachable revolving nosepiece including optical objective lenses, and an inverted SAM including a receiver and/or transmitter, and a specimen holder allowing x-y-z motions.

An acoustic lens was used to form a point focus within the specimen. The point focus acoustic lens comprises a piezoelectric transducer (*i.e.*, zinc oxide) and a buffer rod made of a single crystal of sapphire. The piezoelectric transducer located on the top of the buffer rod was driven in the continuous wave mode at a single frequency. The excitation voltage at the transducer was approximately 5 volt peak-to-peak. The electrical signal was converted into an acoustic signal (*i.e*., ultrasonic plane wave) by the transducer. The shape of the transducer was substantially circular with a diameter of 1mm and a thickness of about 10 μm respectively. The maximum output from the transducer was measured at 185 MHz. The ultrasonic plane wave traveled through the buffer rod to a spherical recess (hereinafter called simply the "lens") located at the bottom of the buffer rod. The lens contained a silicon-oxide layer to form an acoustic impedance matching layer (*i.e.*, acoustic anti-reflection coating) for coupling into water. The diameter of the lens aperture was 843 μm, the aperture angle 120º, and the working distance was 310 μm.

A thin (100) silicon plate (thickness 75 μm) was used as a specimen. The back surface of the specimen was above the lens with its normal along the lens Z-axis. The front and back surfaces of the specimen had been mechanically polished to provide a well characterized boundary. The ultrasonic beam was focused onto a predetermined interior or exterior plane of the specimen by controlling the standoff distance between the lens and the back surface. A special filling apparatus was designed to keep the water coupling in place over periods of a week or more with out refilling. The water temperature was substantially kept at 23ºC.

The laser interferometer utilized a CW 532 nm Nd:YAG laser and a photorefractive interferometer based on Bismuth Silicon Oxide. Data acquisition was synchronized to the source excitation so that complete determination was made of the ultrasonic normal displacement amplitude and phase spatially along the sample front surface plane. With a 20X optical objective, the field of view was about 300 μm, and the spatial resolution was on the order of 1-2 μm.

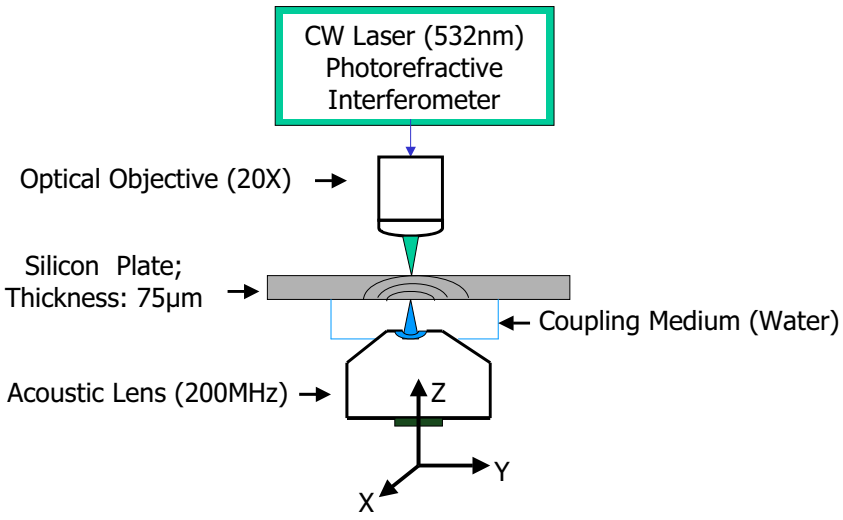

FIGURE 1. A schematic diagram of an optoacoustic system.

Experimental and Theoretical Results

Figure 2 shows the focusing geometry for the measurements, defining the standoff distance Z_F. This distance was varied to change the acoustic lens focal point from outside to inside the material plate. The zero point for Z_F is a location about 600μm below the plate front surface, as shown. When $Z_F = +200$ μm, the focal point is calculated to be at the plate back surface. At each standoff distance, the ultrasonic displacement was recorded at the plate front surface by scanning the sample under the optical objective. Although the system employed can image the data without scanning, the low signal to noise level observed precluded imaging for the excitation levels employed.

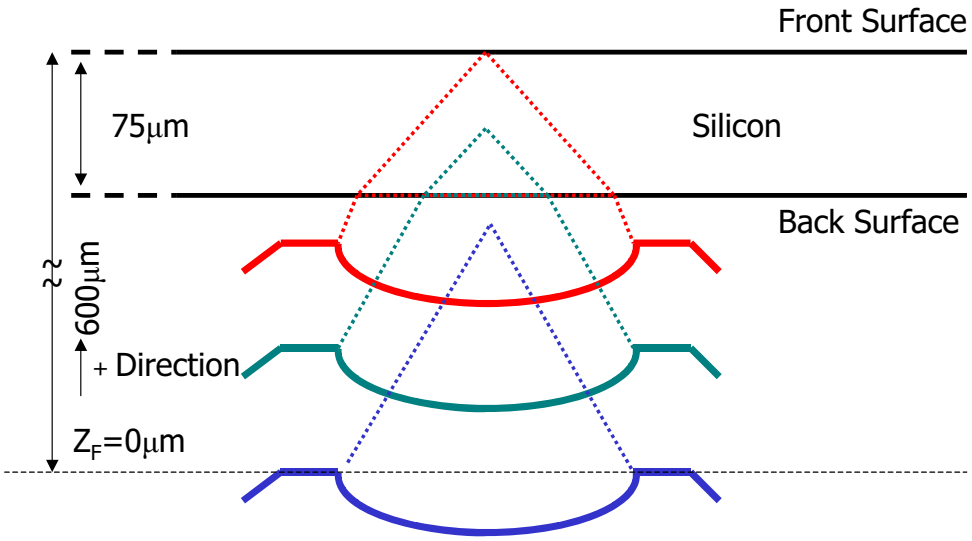

FIGURE 2. Focusing geometry showing the focal distance variable Z_F that is varied from –891μm to +300μm to produce focal points outside and inside the material plate. The origin Z_F = 0 is 600μm from the front surface of the silicon plate.

Figure 3(c) shows the images when the acoustic lens is substantially focused onto the back surface of the specimen. The focal beam spot (the circle at the center) having the maximum intensity is clearly observed. Figure 3(d) shows the phase velocities and wave slowness diagrams for Si(100) and illustrates the variety of wave propagations possible. Also shown is the slowness diagram for S_0 mode plate waves as a function of propagation direction along the plate surface. At the high frequency employed, the S_0, A_0 and Rayleigh modes all coincide. The images of the acoustic wavefronts have essentially the same symmetry properties as the wavenumber as a function of propagation direction, since the material is cubic. Comparison of the acoustic displacement amplitude with the wavenumber prediction for Si(100) shows this similarity in Fig. 3(d).

Figures 3(e) and 3(f) are the experimental and theoretical images when the acoustic lens is mechanically moved toward the front surface from the back surface plane, which would place the focal point above the front surface. Since the aperture angle of the lens is large, longitudinal, shear and surface acoustic waves are all generated when defocusing the lens toward the specimen. Also, since the excitation is continuous, plate wave modes are present due to multiple reflections from the surfaces. Figures 3(e) shows all wave amplitudes

simultaneously; therefore, only through mathematical modeling can discrimination be accomplished between the various types of waves shown in the image.

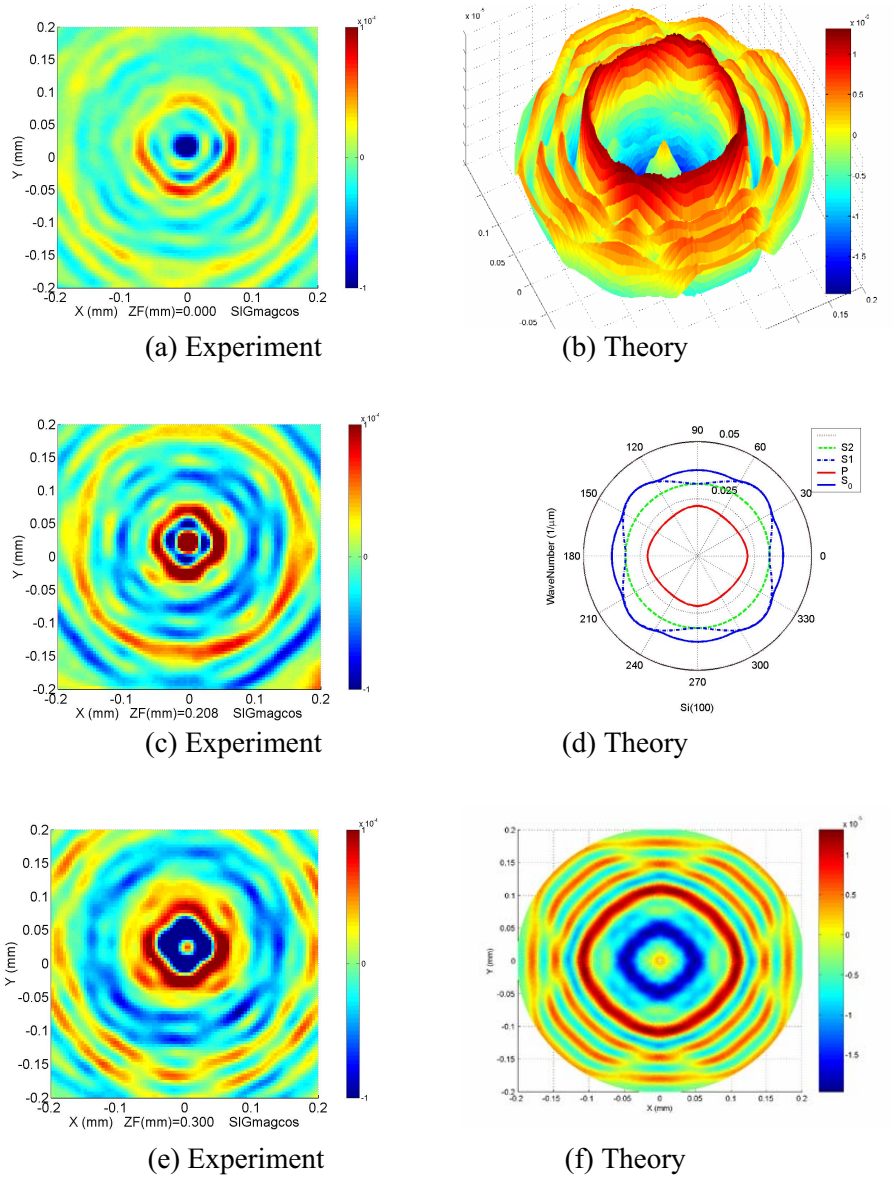

FIGURE 3. Images of the ultrasonic motion (magnitude x cosine (phase)) at the surface as the standoff distance Z_F is changed as indicated..

Conclusions

We presented a hybrid acoustic imaging technique to directly visualize amplitude of acoustic waves propagating within a thin silicon (100) plate as a complimented approach to the conventional SAM. The technique comprises a laser based acoustic microscopy and a mechanical scanning acoustic reflection microscopy. A high frequency acoustic point focus lens (~200 MHz) was used to form a small point source within the plate. Distinct symmetric amplitude patterns were observed as the acoustic focal point moved toward the front surface of the plate. We are planning to use a newly designed acoustic lens for generating large amplitude of ultrasonic waves with higher frequency to form their clearer visualization without mechanical scanning.

We have also developed a mathematical model (*i.e.*, a method of angular spectrum for a plane wave) to calculate an elastic wave field for prediction of acoustic behavior of isotropic and/or anisotropic materials. The computer simulation results based on the model have been compared to the experimental results and .had good agreement.

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